

# Unfolding of the vortical amplification of the magnetic field at inward shocks of Supernova remnant Cassiopeia A

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# Supernova Remnants: Multi-epoch observations

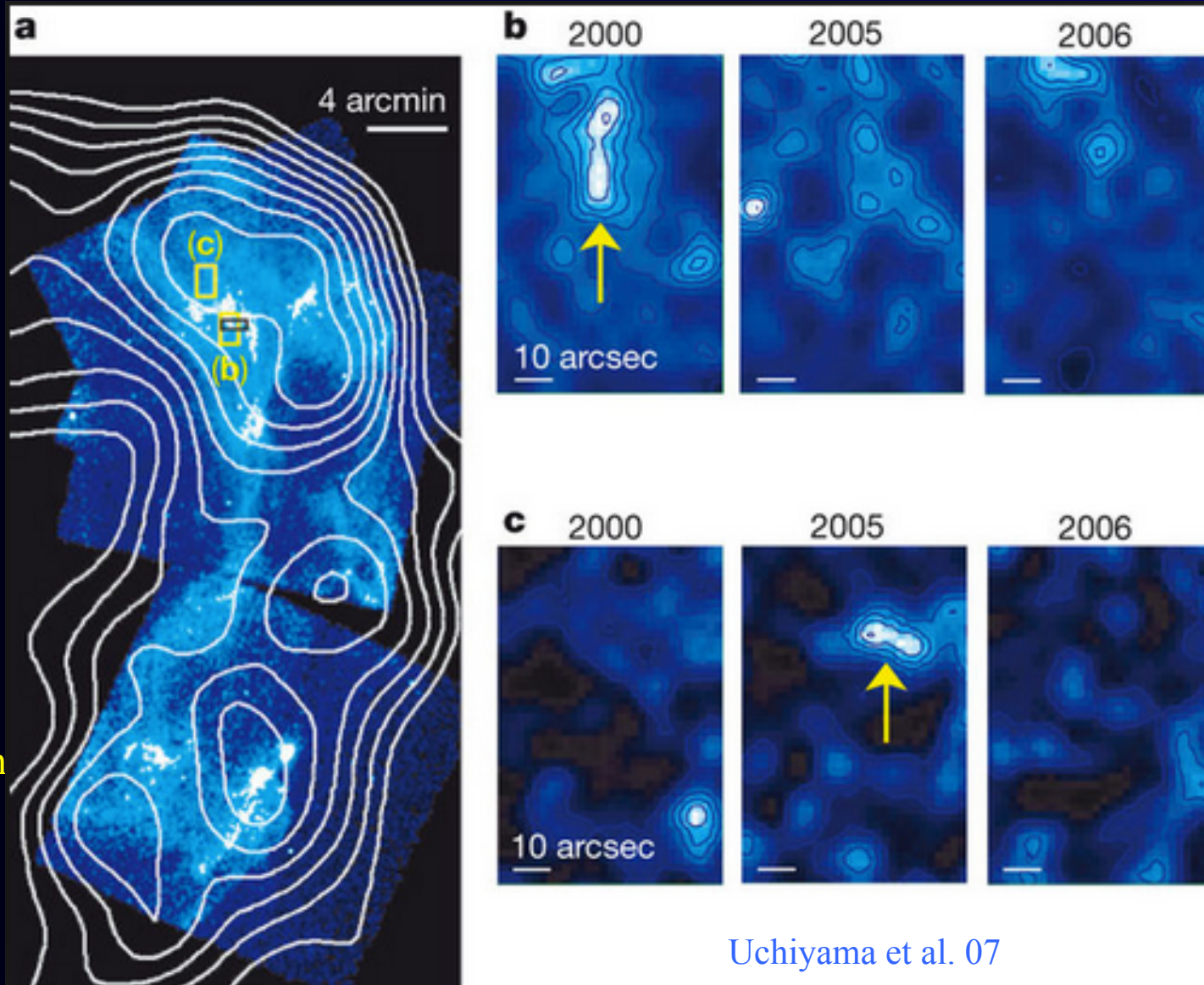
Case of  
RX J1713.7-3946

Chandra:



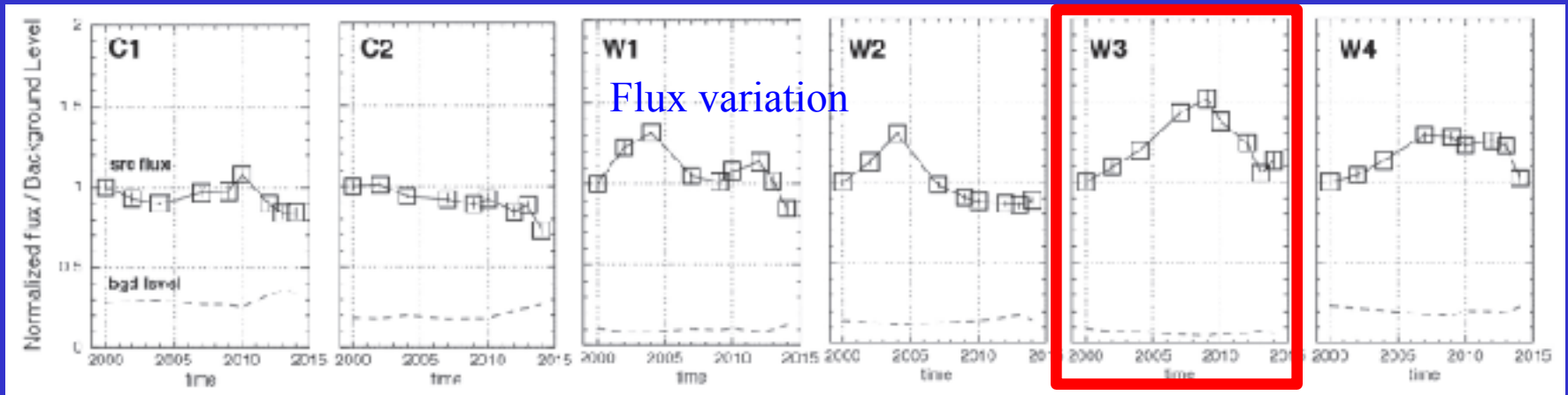
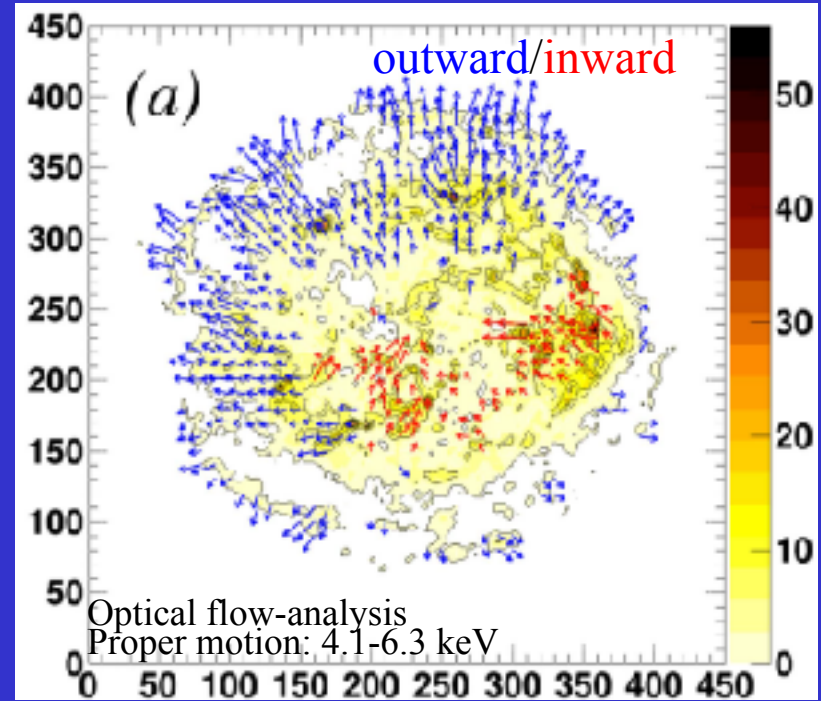
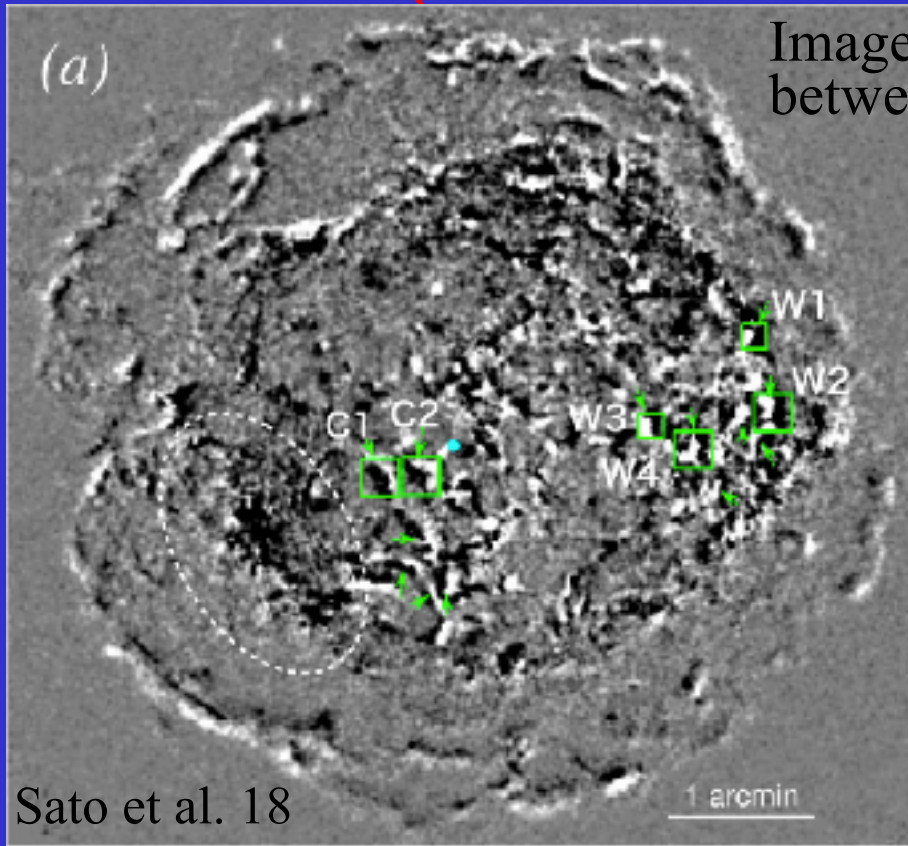
Bright highly  
time-variable  
spots  $\sim 0.01$  pc:

Evidence of  
fast particle acceleration  
and of  $B \sim$  mG  
(strong amplification)



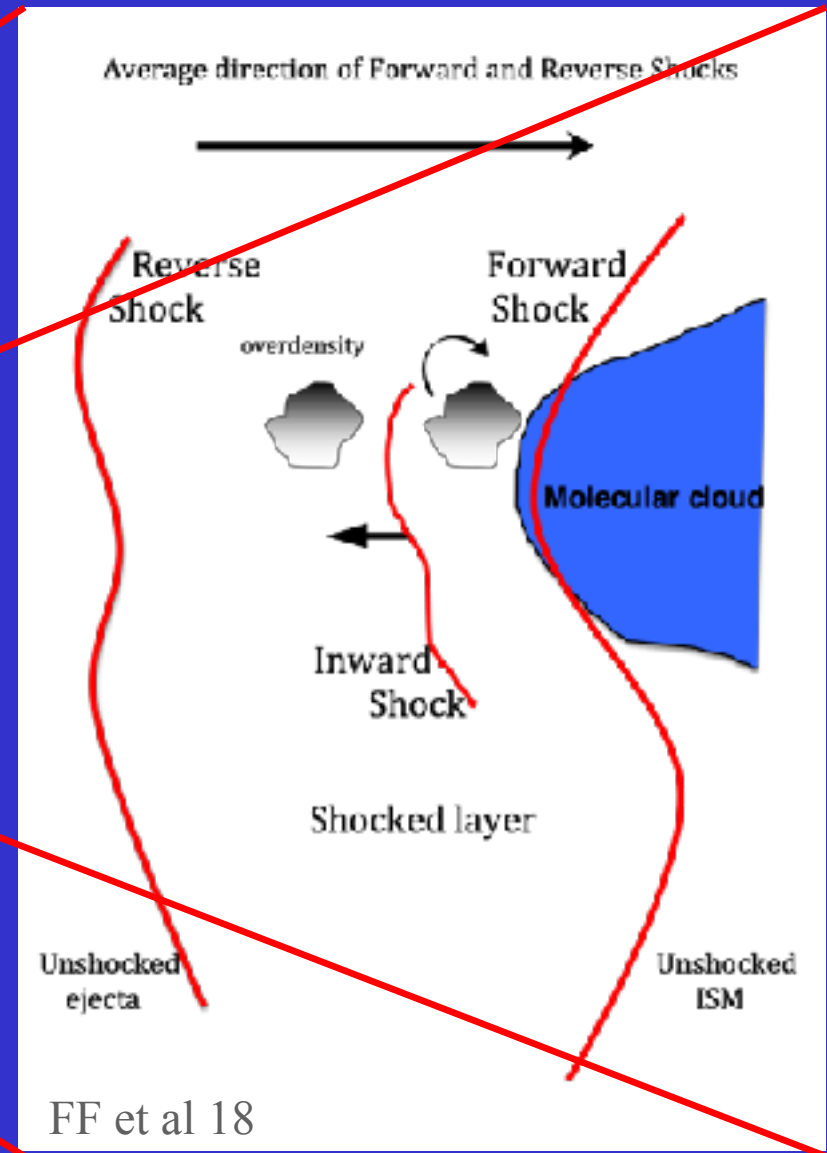
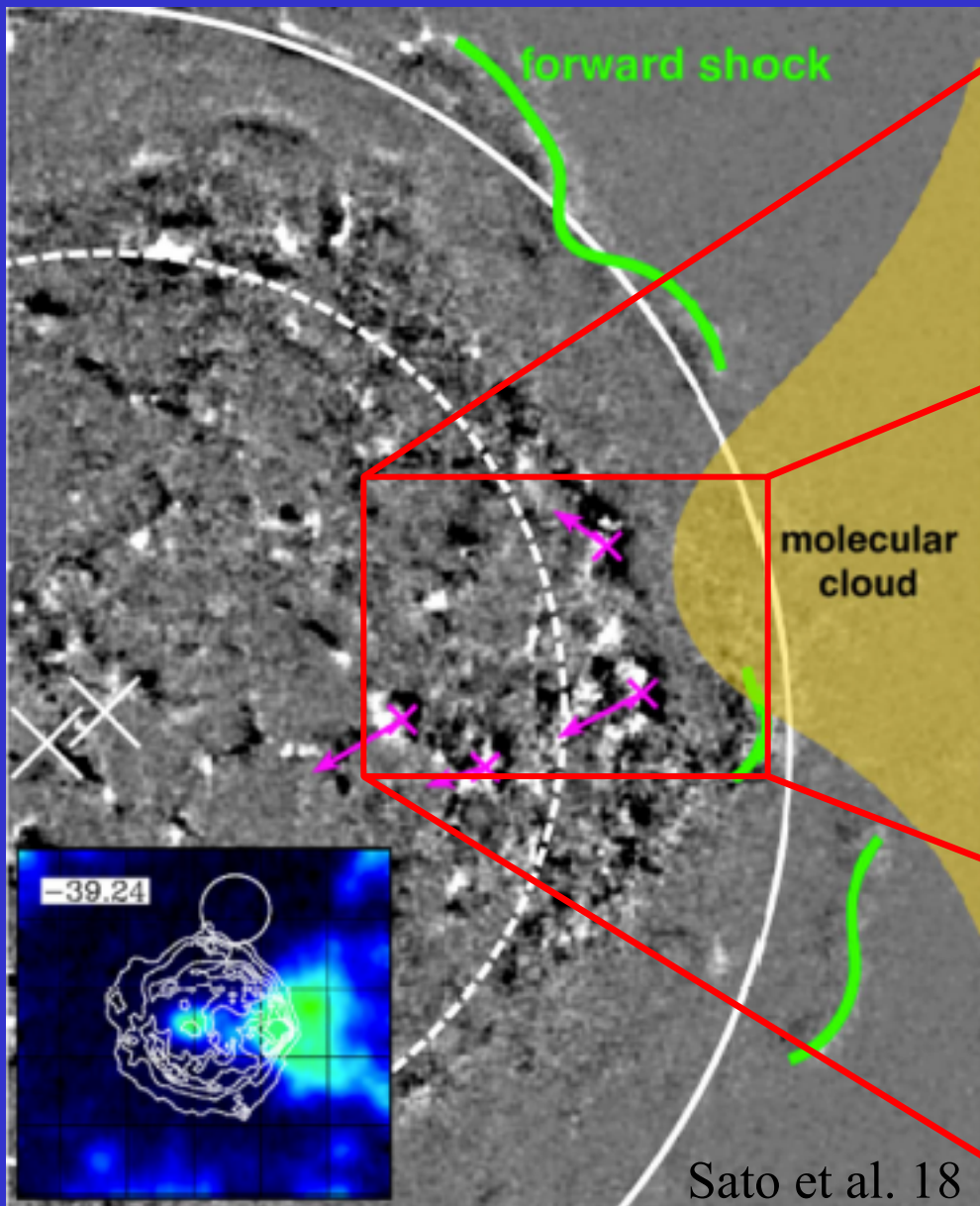
Uchiyama et al. 07

# Cas A (Central/West): Inward shocks



# Inward shock/turbulent medium

Can flux increase be generated by magnetic enhancement only?



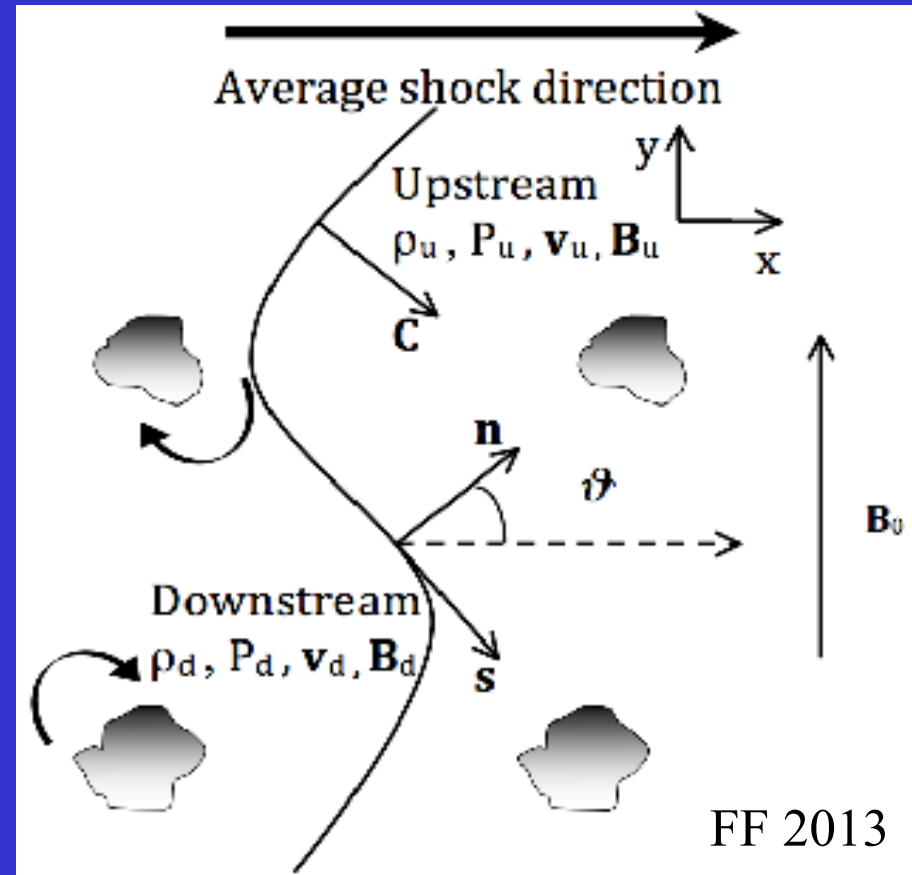
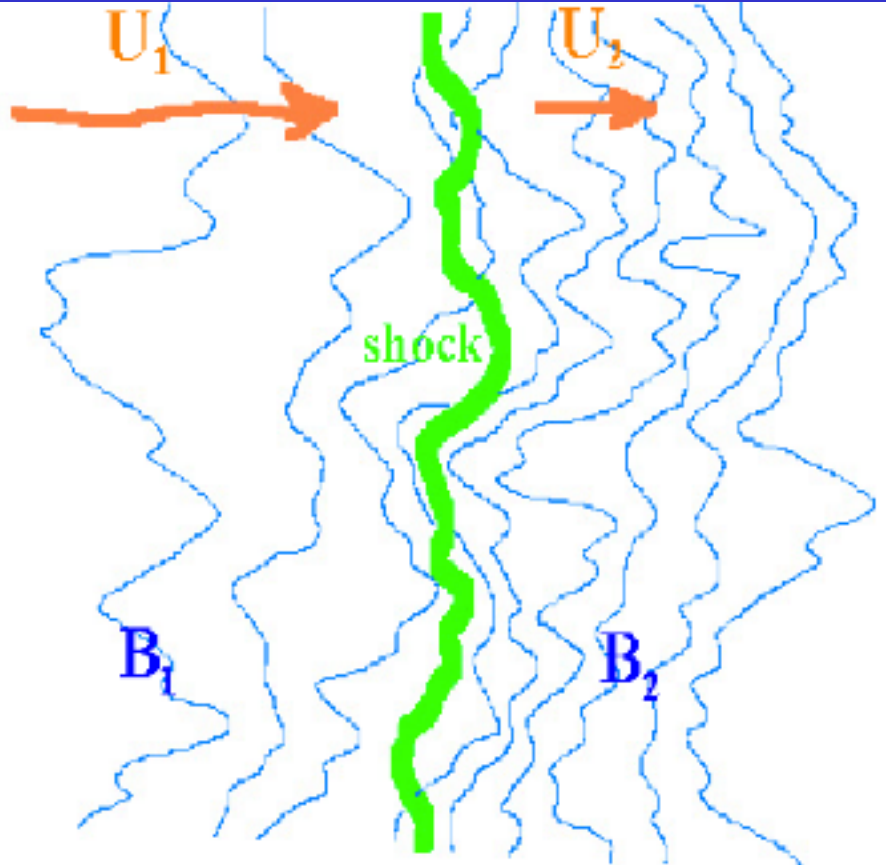
# Jump conditions

Ordinary Rankine-Hugoniot jump conditions cannot be applied to a rippled shock

Local orthonormal frame can be defined:

To first order in  $\theta$   
(large curvature radius)

Perpendicular field upstream



# Vorticity downstream

Non-linear but can be computed analytically

$$\delta\omega_z = \frac{r-1}{r} \left[ \left( \frac{C_r}{\rho} \right)_u \partial_s \rho + \partial_s C_r \right] - \frac{B_n \delta B_s}{4\pi \rho C_r} \partial_s \vartheta$$

$r$ : compression,  $C_r$ : shock speed

FF 2013

Baroclinic term

$$\frac{\partial \omega}{\partial t} = \nabla \times (\mathbf{v} \times \omega) - \frac{\nabla \rho \times \nabla P}{\rho^2}$$

Energy deposited in vortical motion grows with shock speed  
Shear or power spectrum

Finite curvature radius (zero for planar shock)

Turbulent field backreaction  
Strongly rippled  $\rightarrow$  higher amplified field  
Large  $B_0$  makes resistance to field lines tangling

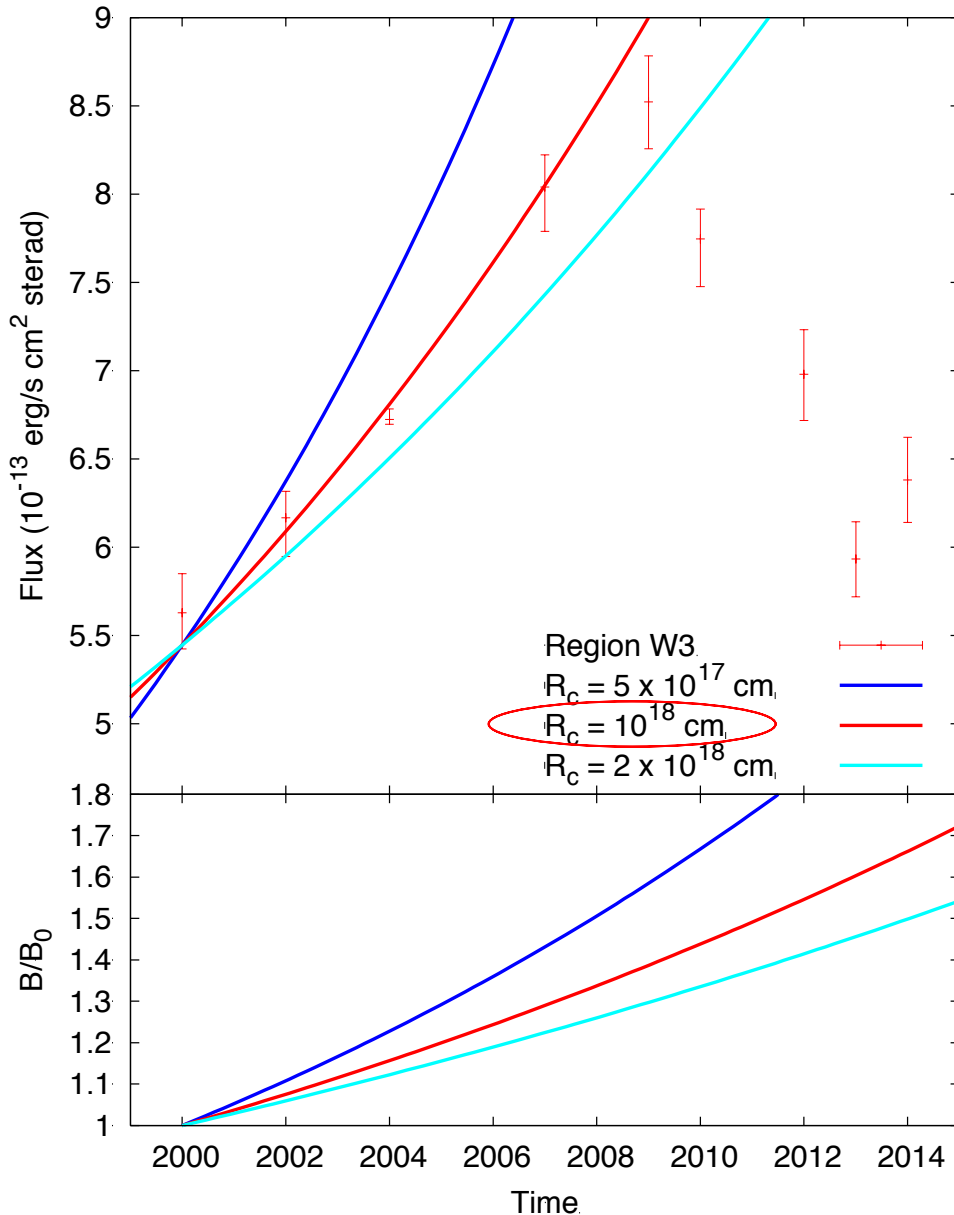
growth rate

backreaction

$$\frac{\varepsilon}{\varepsilon_0}(t) = \left( \frac{B}{B_0} \right)^2 (t) = \frac{e^{2t/\tau}}{1 - \alpha\tau(1 - e^{2t/\tau})v_A^2/2}$$

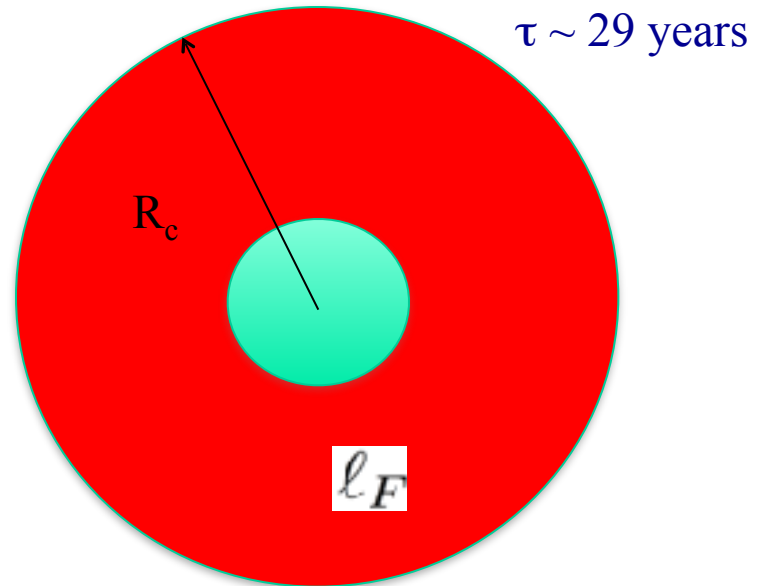
$$\tau \sim \frac{r}{r-1} \frac{1}{C_r} \frac{R_c \ell_F}{R_c + \ell_F} \sim \frac{\ell_F}{C_r}$$

# Flux increase



Synchrotron flux with  $B = B(t)$

Shock speed, compression (i.e., spectral index), photon energy determined by observations; only two free parameters:  $R_c$  and  $\ell_F$



Flux increase might be related to a slow particle acceleration, instead of B-growth, or to a B-growth due to a different mechanism

# Conclusion

Shocks in nature cross inherently turbulent media.  
This affects the diffusion of charged particles at shocks

Multi-epoch monitoring (Chandra) of shock/molecular cloud interactions provides us with invaluable information of the dynamics at shocks and can be quantitatively related to enhancement of magnetic energy

The turbulence scales as the Alfvén Mach number (of order of a few unities). Consistent with not very strong turbulence generated here (diffusion coefficient different from Bohm limit).